



Research Article

## Performance optimization of a horizontal axis wind turbine simulator under the effects of blade's pitch angle variation

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### Article Info

### Abstract

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The optimization of wind turbine performance is a critical issue for enhancing energy conversion efficiency. This study investigates the effects of blade pitch angles and Variable Frequency Drive settings on the performance of a wind turbine system using the Spectra Quest wind turbine simulator. Employing a Taguchi design of experiments with a full factorial approach, a total of 81 experimental tests are conducted to analyze the influence of three blade pitch angles (0°, 10°, and 20°) combined with three distinct Variable Frequency Drive settings (12, 15, and 18) on shaft rotational speed, power output, and vibration levels. Using Taguchi's response analysis and analysis of variance, this research identifies Variable Frequency Drive as the most influential factor on turbine performance metrics. Regression modelling further elucidates the complex relationships between the operational parameters and performance outcomes. The results reveal significant interactions between the input parameters and demonstrate that lower blade pitch angles in conjunction with higher Variable Frequency Drive settings maximize both shaft rotational speed (171 rpm) and power output (24.102 W), maintaining acceptable vibration levels. The best pitch angle input parameters are found to be  $\beta_1=0^\circ$ ,  $\beta_2=0^\circ$  and  $\beta_3=0^\circ$  with a VFD setting of 18. A notable increase in air resistance at higher pitch angles corroborates the findings of previous studies, highlighting the need for optimal parameter settings to enhance turbine efficiency.

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## 1. Introduction

The increasing reliance at renewable power sources marked a significant transition in worldwide strength strategies aimed toward mitigating weather change and lowering dependence on fossil fuels. Among numerous renewable technologies, wind energy has emerged as one of the maximum promising solutions due to its sustainability, low environmental impact, and potential for scalability. The international installed wind energy capability has grown drastically in recent years, accomplishing 837 GW throughout 31 nations in 2021 [1]. This expansion has caused considerable CO<sub>2</sub> emission reductions, with projections signifying wind power should account for over 30% of the worldwide energy era via mid-century [2]. The industry has visible technological improvements, such as larger turbines and accelerated efficiencies [3]. By 2017, wind strength had turned out to be the second-largest form of power technology in Europe [4]. Despite demanding situations, projections endorse international wind power capacity may want to attain 5800 GW by 2050 [5].

The outcomes of blade pitch angles and rotor speeds on wind turbine performance have been considerably studied using simulations and experimental techniques [6]. Research showed that varying pitch angles and angular velocities significantly affect turbine overall performance parameters which include power output, torque, and performance [7]. For a horizontal-axis wind

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turbine, optimal pitch angles exist for maximum energy technology at given wind velocities [8]. In Darrieus-type turbines, a small negative valued fixed pitch angle could improve performance, although variable-pitch blades can enhance starting torque and efficiency at lower tip speed ratios [9][10]. Experimental studies on a horizontal wind turbine with NACA 6412 airfoils at low wind speeds revealed that an 8° pitch angle produced higher electrical power and total efficiency [11]. Multiple studies employed Taguchi-based design of experiments to analyze the effects of various parameters on turbine efficiency [12]. Wind speed and blade number also significantly impact turbine performance, with optimal results observed at higher wind speeds and 5-blade configurations [13]. The Taguchi method, sometimes combined with Grey Relational Analysis, proved effective for both parameter and tolerance design optimization [14]. Tittus and Diaz (2020) analyzed a turbine performance for different blade tip sizes and twist angles and found that drag and lift coefficients had less significance compared to other parameters [15]. Bossanyi (2003) proposed individual blade pitch control as a method for significant load reduction in pitch-regulated turbines [16]. Firman Aryanto et al. (2013) investigated the impact of wind speed and blade number variations on horizontal-axis wind turbine performance, concluding that the best efficiency was achieved with 5 blades at 4 m/s wind speed [13]. Labib, A.M., et al. (2020) examined the effect of blade angle variation on the aerodynamic performance of a horizontal axis wind turbine using computational simulation and experimental validation [17]. Gumilar, L. et al. (2020) revealed that increasing the pitch angle of a horizontal-axis wind turbine decreases the maximum power produced [18]. These findings highlighted the importance of optimizing blade pitch angles and rotor speeds to enhance wind turbine performance across various designs and operating conditions [19].

The value of this study lies in its systematic investigation of ways varying blade pitch angles and VFD settings have an impact on vital performance measures, particularly shaft rotational speed, energy output, and vibration levels. By addressing this subject matter, the interplay of these parameters and their implications for wind turbine design and operation may be explored. The primary objectives of this study are to: 1) analyze the outcomes of different blade pitch angles and VFD settings on the performance of a wind turbine system, 2) offer an in-depth statistical evaluation of the records through Taguchi's response evaluation and regression modelling techniques, and 3) optimize the operational parameters to maximize strength output at the same time as minimizing vibration problems.

This article is structured as follows: section 2 discusses the methods and materials employed, detailing the experimental design, data collection process, and analytical techniques used. Section 3 highlights the results and discussion including the experimental measurements and their analysis, Taguchi design response analysis, analysis of variance (ANOVA) from regression modelling and finally optimization using Grey Relational Analysis of best-fit responses with optimal parameter settings [20][21]. Finally, section 4 summarizes the conclusions with key contributions of this research work, suggests practical implications, and outlines directions for future research in the domain of wind energy optimization.

## **2. Methods and Materials**

### **2.1 Experimental Set-Up**

This section outlined the methodology employed in this research. The WTS model used in this research study was the Spectra Quest (SQ) type that used a Vibra Quest (VQ) simulation software and data acquisition system, shown in Figs 1 and 2. The SQ WTS weights 222.7 kg, has a centerline height of 2.369 m, a sweeping blade diameter of 3.3 m, and base measurements of 2.991 m × 2.438 m. On the rotational shaft, a tachometer and an accelerometer were installed to detect the vibration level and rotational speed in one direction of vibrational excitation, respectively.



Fig. 1. SQ WTS

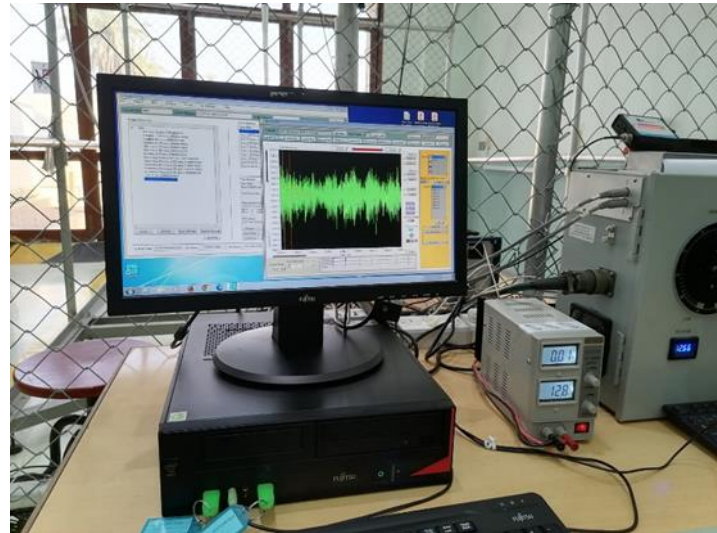


Fig. 2. VQ analysis software

## 2.2 Taguchi Design of Experiment

The analysis was predicated on four critical input parameters:

- The pitch angles of the three blades were varied systematically. Each pitch angle was selected from three distinct levels to examine the effects of adjustment.
- The variable frequency drive (VFD) controlled the rotational speed of the turbine shaft. Three different VFD settings were utilized to create varied operational conditions. The running conditions emphasized that the turbine would operate under varying shaft rotational speeds due to input parameters.

Studying pitch angles from  $0^\circ$  to  $30^\circ$  strikes a balance between capturing meaningful aerodynamic and structural behavior and avoiding overly complex or unrealistic scenarios. This range is particularly relevant for applications involving lift, drag, energy capture, and load control. This confirms practical visions for engineering design and analysis. The Taguchi design of experiments DoE with a full factorial approach was used to plan the experimental work. There are four input parameters,  $\beta_1$ ,  $\beta_2$ ,  $\beta_3$  and VFD. Taguchi design of experiments with a full factorial approach was used to plan the experimental works. The Experimental layout was based on  $L_{81} (3^4)$  orthogonal array. To design the Experimental layout based on this  $L_{81} (3^4)$  orthogonal array, three levels were required for each input parameter. The determining pitch angle variations were  $0^\circ$ ,  $10^\circ$  and  $20^\circ$ , which were selected within the pitch angle range, with equal increments in between. The four input parameters each had three levels are shown in Table 1. The responses were the shaft rotational speed, vibration level and power output.

The blade angles were changed using pitch control software, shown in Fig. 3. The initial setting was when  $\beta_1=0^\circ$ ,  $\beta_2=0^\circ$  and  $\beta_3=0^\circ$ . Both the initial and maximum settings of the angles are shown in Fig. 3. The Variable Frequency Drive (VFD) was set for three levelling values; 12, 15 and 18, as shown in Fig. 4.

Table 1. Experimental input parameters and their levels

| Factor    | Name                     | Levels    |            |            |
|-----------|--------------------------|-----------|------------|------------|
| $\beta_1$ | Blade 1 Pitch Angle      | $0^\circ$ | $10^\circ$ | $20^\circ$ |
| $\beta_2$ | Blade 2 Pitch Angle      | $0^\circ$ | $10^\circ$ | $20^\circ$ |
| $\beta_3$ | Blade 3 Pitch Angle      | $0^\circ$ | $10^\circ$ | $20^\circ$ |
| VFD       | Variable Frequency Drive | 12        | 15         | 18         |

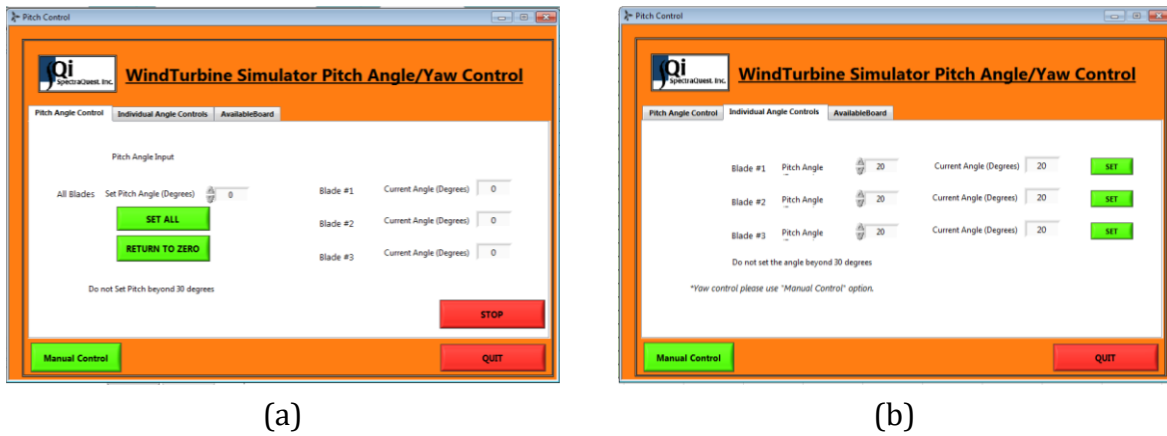


Fig. 3. Setting of blade angles (a) Initial setting and (b) maximum setting)

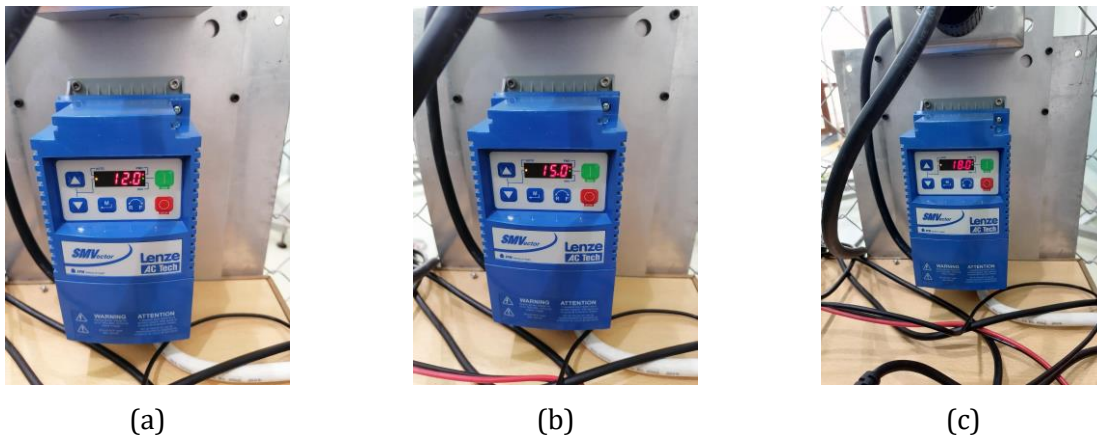


Fig. 4. VFD settings (a) 12, (b) 15 and (c) 18

### 2.3 Experimental testing of the WTS as per DoE

This involved a systematic change of the pitch angle of each blade, starting first with 0° pitch angle for all three blades, setting the VFD to 12 and performing the experiment. The shaft rotational speed, vibration level and power output were measured and recorded using a mounted tachometer, accelerometer and a 3-phase field-controlled alternator, respectively. Then, the VFD setting was changed to 15 then 18, and the experiment was performed again for each VFD setting. After that, the pitch angles were changed as per the design of experiment and the experimental work was performed for 81 tests.

### 2.4 Results Analysis

The results of 81 experiments were analyzed to investigate the effects of changing pitch angles on the shaft rotational speed, vibration level and power output. The Vibra Quest software generated the vibration waveform reports in MS Excel format. At higher angles, the air resistance was expected to play a negative role on rotational speed and power output. Simultaneously and at certain combinations of pitch angles, the wind turbine was expected to undergo a balancing scenario at which the vibration level decreased within the same setting of VFD.

### 2.5 Regression Modelling:

The regression modelling for the three responses was performed using Minitab software to develop the best fit regression models, considering the R-squared values for each response.

### 2.5 Optimization

The multi-responses of this research work were optimized using Grey Relational Analysis. For the shaft rotational speed and power output, the higher-the-better criterion was used. While, for vibration level, the lower-the-better criterion was used. The normalization of the original sequence of each response was calculated as follows:

$$\text{For higher-the-better criterion: } Y_{ij} = \frac{x_{ij} - \min(x_{ij})}{\max(x_{ij}) - \min(x_{ij})} \quad (1)$$

$$\text{For lower-the-better criterion: } Y_{ij} = \frac{\max(x_{ij}) - x_{ij}}{\max(x_{ij}) - \min(x_{ij})} \quad (2)$$

where  $x_{ij}$  is the measured response,  $\min(x_{ij})$  is the minimum of  $x_{ij}$  and  $\max(x_{ij})$  is the maximum of  $x_{ij}$ ,  $i$  is the response variables and  $j$  is the experiment number. The Deviation Sequence (distinguishing coefficient)  $\Delta_{ij}$  was calculated as follows:

$$\Delta_{ij} = \max(Y_{ij}) - Y_{ij} \quad (3)$$

where  $\max(Y_{ij})$  is the expected sequence,  $Y_{ij}$  is the comparability sequence and  $\Delta_{ij}$  is the deviation sequence of  $\max(Y_{ij})$  and  $Y_{ij}$ . The grey relational coefficient  $\xi_{ij}$  was calculated as follows:

$$\xi_{ij} = \frac{\min(\Delta_{ij}) + \zeta \times \max(\Delta_{ij})}{\Delta_{ij} + \zeta \times \max(\Delta_{ij})} \quad (4)$$

where  $\zeta$  is the differentiating coefficient,  $0 \leq \zeta \leq 1$ , and 0.5 is the widely accepted value. The grey relational grade GRG ( $\gamma_j$ ) for each experiment was computed as follows, for n number of responses:

$$\gamma_j = \frac{\sum_{i=1}^n \xi_{ij}}{n} \quad (5)$$

If larger  $\gamma_j$  is obtained, then the equivalent set of process parameters is nearer to the most favorable optimal setting.

## 3. Results and Discussion

The results of the experimental tests using the Spectra Quest Wind Turbine Simulator (SQ WTS) are presented in this section. This detailed the effects of varying the pitch angles of the blades under different settings of Variable Frequency Drive (VFD) on shaft rotational speed, power output, and vibration levels.

### 3.1 Experimental Overview

A total of 81 experiments were conducted based on the Taguchi design of experiments approach using a full factorial design with  $L_{81}(3^4)$  orthogonal array. Each experiment was systematically designed to assess the impact of the three blade pitch angles' combinations ( $0^\circ$ ,  $10^\circ$ , and  $20^\circ$  for each of the three blades) and three Variable Frequency Drive (VFD) settings (12, 15, and 18). Table 2 shows the measured responses of the experimental work.

Table 2. Measured responses from experimental tests

| Exp | Input Parameters       |                        |                        |     | Measured responses |                  |                                     |
|-----|------------------------|------------------------|------------------------|-----|--------------------|------------------|-------------------------------------|
|     | $\beta_1$ ( $^\circ$ ) | $\beta_2$ ( $^\circ$ ) | $\beta_3$ ( $^\circ$ ) | VFD | Rot. Spd. (rpm)    | Power Output (W) | Vibration Level (m/s <sup>2</sup> ) |
| 1   | 0                      | 0                      | 0                      | 12  | 112                | 10.730           | 6.274                               |
| 2   | 0                      | 0                      | 0                      | 15  | 141                | 17.430           | 10.106                              |
| 3   | 0                      | 0                      | 0                      | 18  | 171                | 24.102           | 10.326                              |
| 4   | 0                      | 0                      | 10                     | 12  | 111                | 10.643           | 6.943                               |
| 5   | 0                      | 0                      | 10                     | 15  | 139                | 16.898           | 11.238                              |

Table 2 (continued)

| Exp | Input Parameters |               |               |     | Measured responses |                  |                                     |
|-----|------------------|---------------|---------------|-----|--------------------|------------------|-------------------------------------|
|     | $\beta 1$ (°)    | $\beta 2$ (°) | $\beta 3$ (°) | VFD | Rot. Spd. (rpm)    | Power Output (W) | Vibration Level (m/s <sup>2</sup> ) |
| 6   | 0                | 0             | 10            | 18  | 168                | 23.868           | 10.849                              |
| 7   | 0                | 0             | 20            | 12  | 107                | 10.237           | 7.486                               |
| 8   | 0                | 0             | 20            | 15  | 134                | 16.014           | 10.239                              |
| 9   | 0                | 0             | 20            | 18  | 157                | 21.164           | 10.411                              |
| 10  | 0                | 10            | 0             | 12  | 110                | 10.701           | 7.400                               |
| 11  | 0                | 10            | 0             | 15  | 139                | 17.290           | 11.402                              |
| 12  | 0                | 10            | 0             | 18  | 167                | 23.868           | 10.760                              |
| 13  | 0                | 10            | 10            | 12  | 109                | 10.382           | 7.352                               |
| 14  | 0                | 10            | 10            | 15  | 137                | 16.558           | 11.181                              |
| 15  | 0                | 10            | 10            | 18  | 164                | 22.610           | 10.354                              |
| 16  | 0                | 10            | 20            | 12  | 106                | 9.688            | 8.013                               |
| 17  | 0                | 10            | 20            | 15  | 131                | 15.015           | 9.925                               |
| 18  | 0                | 10            | 20            | 18  | 153                | 20.498           | 10.859                              |
| 19  | 0                | 20            | 0             | 12  | 107                | 10.411           | 8.005                               |
| 20  | 0                | 20            | 0             | 15  | 135                | 16.218           | 11.316                              |
| 21  | 0                | 20            | 0             | 18  | 159                | 22.192           | 10.966                              |
| 22  | 0                | 20            | 10            | 12  | 107                | 10.121           | 7.308                               |
| 23  | 0                | 20            | 10            | 15  | 132                | 15.844           | 10.204                              |
| 24  | 0                | 20            | 10            | 18  | 155                | 20.905           | 10.396                              |
| 25  | 0                | 20            | 20            | 12  | 103                | 9.380            | 8.424                               |
| 26  | 0                | 20            | 20            | 15  | 126                | 14.652           | 8.952                               |
| 27  | 0                | 20            | 20            | 18  | 143                | 17.955           | 11.675                              |
| 28  | 10               | 0             | 0             | 12  | 110                | 10.701           | 7.712                               |
| 29  | 10               | 0             | 0             | 15  | 139                | 17.325           | 12.348                              |
| 30  | 10               | 0             | 0             | 18  | 166                | 23.907           | 10.925                              |
| 31  | 10               | 0             | 10            | 12  | 108                | 10.614           | 7.795                               |
| 32  | 10               | 0             | 10            | 15  | 136                | 16.660           | 12.325                              |
| 33  | 10               | 0             | 10            | 18  | 162                | 23.028           | 11.423                              |
| 34  | 10               | 0             | 20            | 12  | 105                | 10.295           | 6.774                               |
| 35  | 10               | 0             | 20            | 15  | 133                | 15.576           | 7.052                               |
| 36  | 10               | 0             | 20            | 18  | 155                | 21.090           | 10.072                              |
| 37  | 10               | 10            | 0             | 12  | 109                | 10.701           | 10.528                              |
| 38  | 10               | 10            | 0             | 15  | 137                | 16.762           | 7.474                               |
| 39  | 10               | 10            | 0             | 18  | 163                | 23.400           | 12.156                              |
| 40  | 10               | 10            | 10            | 12  | 108                | 10.498           | 10.750                              |
| 41  | 10               | 10            | 10            | 15  | 135                | 16.422           | 7.739                               |
| 42  | 10               | 10            | 10            | 18  | 159                | 22.306           | 11.469                              |
| 43  | 10               | 10            | 20            | 12  | 105                | 10.092           | 10.872                              |
| 44  | 10               | 10            | 20            | 15  | 129                | 15.180           | 8.217                               |
| 45  | 10               | 10            | 20            | 18  | 150                | 20.424           | 9.910                               |
| 46  | 10               | 20            | 0             | 12  | 106                | 10.353           | 11.462                              |
| 47  | 10               | 20            | 0             | 15  | 132                | 15.980           | 8.174                               |
| 48  | 10               | 20            | 0             | 18  | 153                | 20.831           | 10.679                              |
| 49  | 10               | 20            | 10            | 12  | 105                | 10.237           | 11.416                              |
| 50  | 10               | 20            | 10            | 15  | 130                | 15.312           | 8.378                               |
| 51  | 10               | 20            | 10            | 18  | 152                | 22.572           | 10.309                              |

Table 2 (continued)

| Exp | Input Parameters |               |               |     | Measured responses |                  |                                     |
|-----|------------------|---------------|---------------|-----|--------------------|------------------|-------------------------------------|
|     | $\beta 1$ (°)    | $\beta 2$ (°) | $\beta 3$ (°) | VFD | Rot. Spd. (rpm)    | Power Output (W) | Vibration Level (m/s <sup>2</sup> ) |
| 52  | 10               | 20            | 20            | 12  | 103                | 9.240            | 7.490                               |
| 53  | 10               | 20            | 20            | 15  | 128                | 14.080           | 7.599                               |
| 54  | 10               | 20            | 20            | 18  | 143                | 17.710           | 10.287                              |
| 55  | 20               | 0             | 0             | 12  | 108                | 10.440           | 6.916                               |
| 56  | 20               | 0             | 0             | 15  | 137                | 16.558           | 10.124                              |
| 57  | 20               | 0             | 0             | 18  | 162                | 22.534           | 9.982                               |
| 58  | 20               | 0             | 10            | 12  | 107                | 10.237           | 7.081                               |
| 59  | 20               | 0             | 10            | 15  | 134                | 15.444           | 9.469                               |
| 60  | 20               | 0             | 10            | 18  | 157                | 20.905           | 9.675                               |
| 61  | 20               | 0             | 20            | 12  | 104                | 9.660            | 8.354                               |
| 62  | 20               | 0             | 20            | 15  | 128                | 14.652           | 8.630                               |
| 63  | 20               | 0             | 20            | 18  | 146                | 18.720           | 11.268                              |
| 64  | 20               | 10            | 0             | 12  | 106                | 10.034           | 7.744                               |
| 65  | 20               | 10            | 0             | 15  | 133                | 15.378           | 9.940                               |
| 66  | 20               | 10            | 0             | 18  | 156                | 20.646           | 10.647                              |
| 67  | 20               | 10            | 10            | 12  | 105                | 9.520            | 7.942                               |
| 68  | 20               | 10            | 10            | 15  | 130                | 14.916           | 9.354                               |
| 69  | 20               | 10            | 10            | 18  | 152                | 20.128           | 10.513                              |
| 70  | 20               | 10            | 20            | 12  | 101                | 9.184            | 8.862                               |
| 71  | 20               | 10            | 20            | 15  | 124                | 13.760           | 8.772                               |
| 72  | 20               | 10            | 20            | 18  | 140                | 17.535           | 12.254                              |
| 73  | 20               | 20            | 0             | 12  | 103                | 9.296            | 8.976                               |
| 74  | 20               | 20            | 0             | 15  | 127                | 14.718           | 8.951                               |
| 75  | 20               | 20            | 0             | 18  | 147                | 19.152           | 10.863                              |
| 76  | 20               | 20            | 10            | 12  | 102                | 9.100            | 8.739                               |
| 77  | 20               | 20            | 10            | 15  | 125                | 13.952           | 8.912                               |
| 78  | 20               | 20            | 10            | 18  | 142                | 17.920           | 12.414                              |
| 79  | 20               | 20            | 20            | 12  | 99                 | 8.505            | 9.561                               |
| 80  | 20               | 20            | 20            | 15  | 119                | 12.524           | 8.593                               |
| 81  | 20               | 20            | 20            | 18  | 133                | 15.411           | 10.496                              |

### 3.2 Shaft Rotational Speed

The collected experimental results showed varied shaft rotational speeds based on different combinations of input parameters. Fig. 5 shows the graph of shaft rotational speed versus the VFD setting for each combination of blade pitch angles (legend  $\beta 1+\beta 2+\beta 3$ ). For each VFD setting, the rotational speed varied as a result of air resistance on the blade, mostly with higher pitch angles. From the initial blades' angle settings (input parameters) to the final blades' angle settings (input parameters), the rotational speed varied from 99 rpm to 112 rpm at VFD = 12. For VFD = 15, the rotational speed changed from 119 rpm to 141 rpm. While, for VFD = 18, the rotational speed altered from 133 rpm to 171 rpm. The maximum pitch angle settings (20°) marked a decrease in rotational speed. This confirmed the hypothesis that increased blade angle contributes to higher air resistance [22].

### 3.3 Power Output

The power output results reflected similarly the interdependencies of the blade angles and VFD settings, as shown in Fig. 6. This power output was proportionally related to the shaft rotational speed connected to the power alternator by the gearbox. For the angle adjustments of the first blades (input parameters) and the last blades (input parameters), if VFD = 12, the power output

varied from 8.505 W to 10.730 W, if VFD = 15, the power output varied from 12.524 W to 17.430 W, and when VFD = 18, the power output varied from 15.411 W to 24.102 W. An inverse relationship was noted at the maximum blade angle settings (20°), which resulted in reduced power outputs due to increased drag [17].

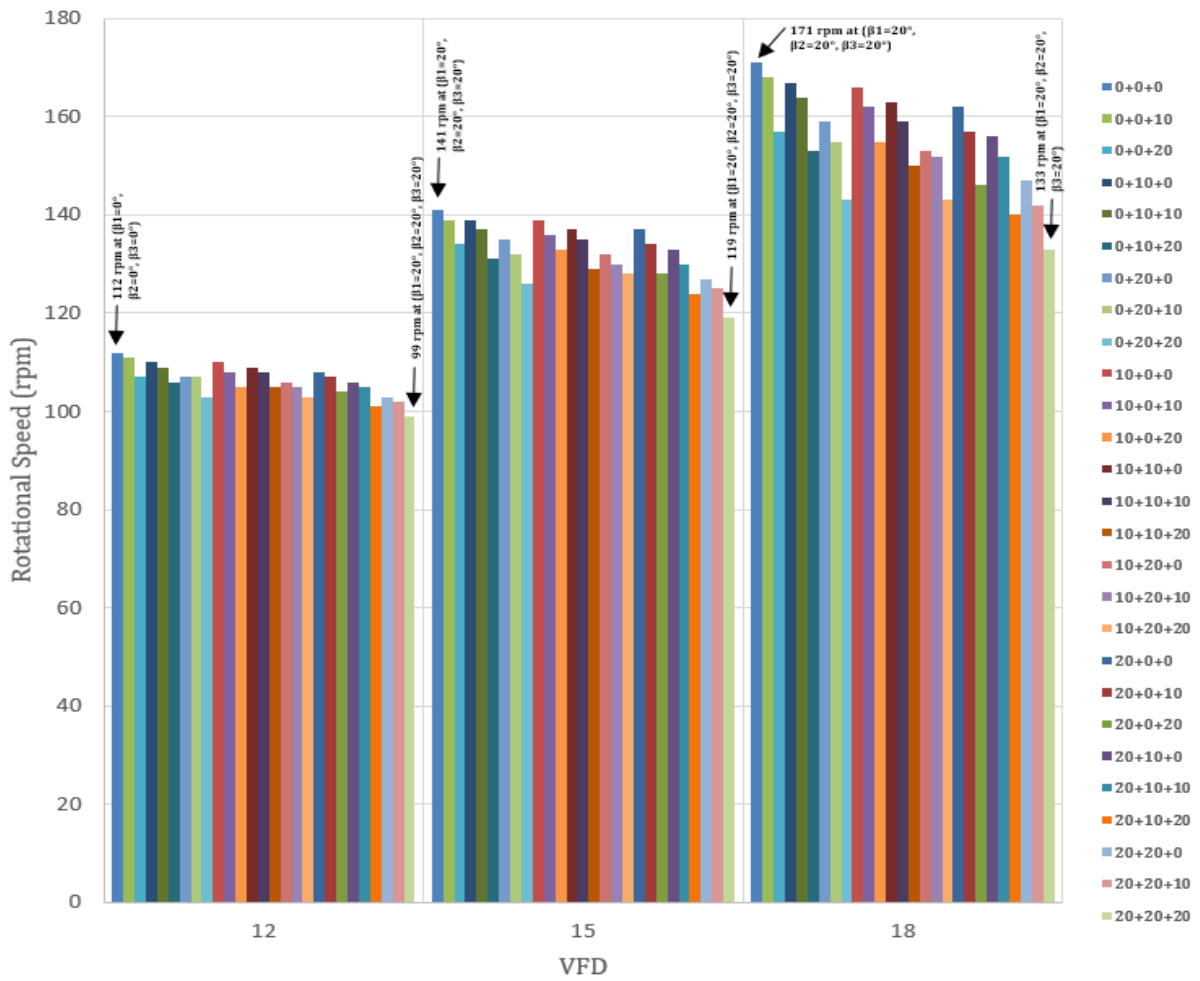


Fig. 5. Variation of shaft rotational speed against the VFD setting (legend  $\beta_1+\beta_2+\beta_3$ )

### 3.4 Vibration Level

The measurements of the vibration levels, as illustrated in Fig. 7, revealed that combinations of higher pitch angles often led to increased vibration levels. However, some specific combinations of pitch angles and VFD settings led to a balancing effect. For example, in VFD = 12, the pitch angle combinations of (experiment 34) showed a vibration level of (6.77 m/s<sup>2</sup>) and (experiment 55) showed a vibration level of (6.92 m/s<sup>2</sup>). These two combinations showed lower vibration levels just above the initial reading of (experiment 1) which was (6.27 m/s<sup>2</sup>). The same for VFD = 15, the pitch angle combinations of (experiment 35), (experiment 38) and (experiment 53) showed much lower vibration levels of (7.05 m/s<sup>2</sup>), (7.47 m/s<sup>2</sup>) and (7.60 m/s<sup>2</sup>) respectively. This is compared to the initial reading of (experiment 1) which was (10.11 m/s<sup>2</sup>). For VFD=18, the pitch angle combinations of (experiment 60), (experiment 45) and (experiment 36) showed much lower vibration levels of (9.68 m/s<sup>2</sup>), (9.91 m/s<sup>2</sup>) and (10.07 m/s<sup>2</sup>) respectively. This is compared to the initial reading of (experiment 1) which was (10.33 m/s<sup>2</sup>). To some extent, the wind turbine system underwent balancing scenarios at these combinations of pitch angles [23].

### 3.5 Taguchi Response Analysis

Taguchi's response analysis focused on optimizing performance metrics through the design of experiments and the minimization of variability. The experimental investigations of blade angle variations on wind turbine systems were analyzed using Taguchi's response analysis, as responses



for means and signal-to-noise ratios. The influence of selected input process parameters on various performance measures like the shaft rotational speed, power output and vibration level are detailed.

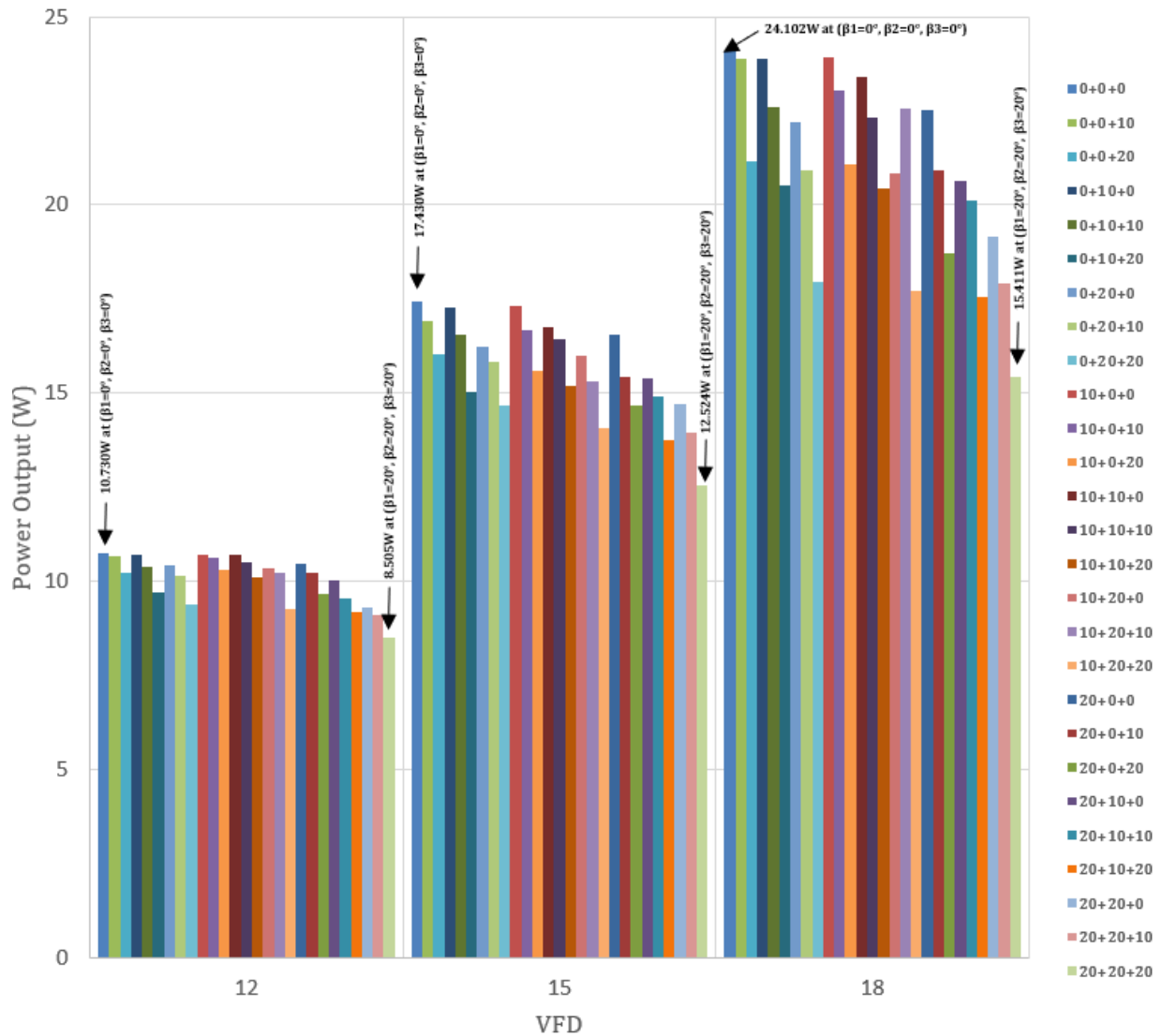


Fig. 6. Variation of power output against the VFD setting (legend  $\beta_1+\beta_2+\beta_3$ )

### 3.5.1 Taguchi's Response Analysis for The Shaft Rotational Speed

In this case, the process parameters  $\beta_1$ ,  $\beta_2$ ,  $\beta_3$  and VFD were analyzed for their effects on the shaft rotational speed. In Table 3, the Mean and Signal to Noise Ratios values illustrated how changes in each factor impact the system's performance. Considering the higher-the-better criterion, the best possible set of process parameters observed from the analysis was  $\beta_1-1$ ,  $\beta_2-1$ ,  $\beta_3-1$  and VFD-3, which means ( $\beta_1=0^\circ$ ,  $\beta_2=0^\circ$ ,  $\beta_3=0^\circ$  and VFD=18). The response graphs for the rotational speed of both Means and Signal to Noise Ratios are shown in Fig. 8.

Table 3. Response table for the shaft rotational speed

| Level | Means     |           |           |       | Signal to Noise Ratios |           |           |       |
|-------|-----------|-----------|-----------|-------|------------------------|-----------|-----------|-------|
|       | $\beta_1$ | $\beta_2$ | $\beta_3$ | VFD   | $\beta_1$              | $\beta_2$ | $\beta_3$ | VFD   |
| 1     | 134.2     | 134.7     | 134.6     | 106.1 | 42.44                  | 42.47     | 42.46     | 40.51 |
| 2     | 131.9     | 131.8     | 132.3     | 132.2 | 42.30                  | 42.29     | 42.32     | 42.42 |
| 3     | 126.9     | 126.5     | 126.1     | 154.6 | 41.97                  | 41.95     | 41.92     | 43.77 |
| Delta | 7.3       | 8.2       | 8.5       | 48.5  | 0.47                   | 0.52      | 0.54      | 3.26  |
| Rank  | 4         | 3         | 2         | 1     | 4                      | 3         | 2         | 1     |

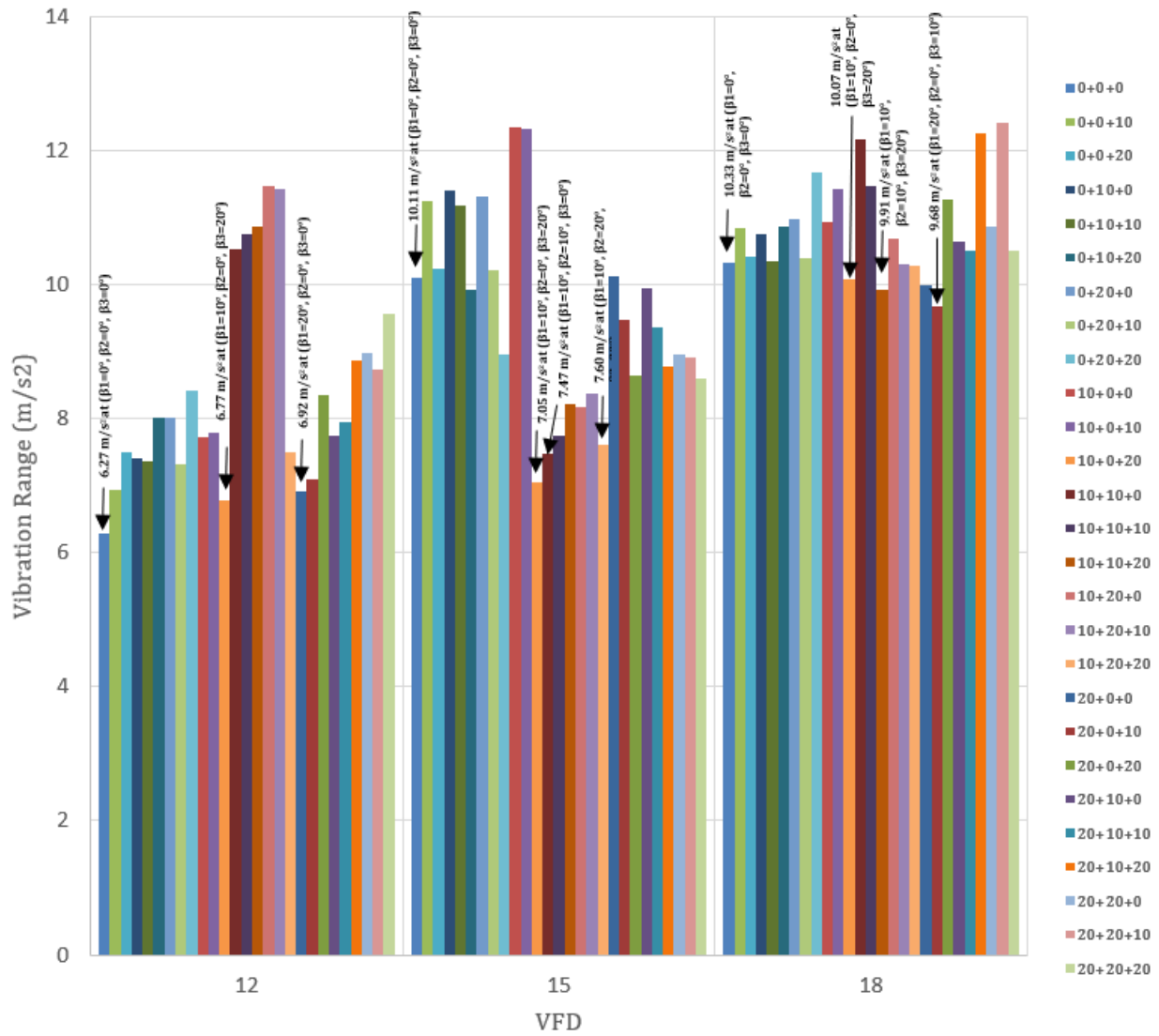


Fig. 7. Vibration levels across different settings (legend  $\beta_1+\beta_2+\beta_3$ )



(a)



(b)

Fig. 8. Response graphs for the shaft rotational speed: (a) Means, 8b) Signal to Noise Ratios

### 3.5.2 Influence of Process Parameters on The Shaft Rotational Speed

Looking at the rankings in Table 4, VFD had the most significant impact on the rotational speed with the highest Delta values (48.5 for Means and 3.26 for S/N Ratios). This indicated that the shaft rotational speed was most sensitive to changes in the VFD settings. The pitch angles  $\beta_3$ ,  $\beta_2$ , and  $\beta_1$  followed in descending order of influence, with  $\beta_3$  showing a slightly higher impact than  $\beta_2$  and  $\beta_1$ .

### 3.5.3 Taguchi's Response Analysis for The Power Output

In this instance, the impact of the process parameters  $\beta_1$ ,  $\beta_2$ ,  $\beta_3$ , and VFD on the power output was examined. Table 5 shows how variations in each factor affect the system's performance through the Mean and Signal to Noise Ratios values. The analysis revealed that the optimal set of process parameters, based on the higher-the-better criterion, was  $\beta_1$ -1,  $\beta_2$ -1,  $\beta_3$ -1, and VFD-3, similar to the shaft rotational speed response with  $\beta_1=0^\circ$ ,  $\beta_2=0^\circ$ ,  $\beta_3=0^\circ$ , and VFD=18. Fig. 9 displays the response graphs for the rotating speed of Means and Signal to Noise Ratios.

Table 4. Response table for the power output

| Level | Means     |           |           |       | Signal to Noise Ratios |           |           |       |
|-------|-----------|-----------|-----------|-------|------------------------|-----------|-----------|-------|
|       | $\beta_1$ | $\beta_2$ | $\beta_3$ | VFD   | $\beta_1$              | $\beta_2$ | $\beta_3$ | VFD   |
| 1     | 16.12     | 16.28     | 16.36     | 10.04 | 23.72                  | 23.81     | 23.85     | 20.02 |
| 2     | 15.97     | 15.69     | 15.84     | 15.60 | 23.66                  | 23.49     | 23.57     | 23.83 |
| 3     | 14.48     | 14.61     | 14.38     | 20.94 | 22.84                  | 22.91     | 22.80     | 26.37 |
| Delta | 1.65      | 1.66      | 1.98      | 10.90 | 0.89                   | 0.90      | 1.05      | 6.35  |
| Rank  | 4         | 3         | 2         | 1     | 4                      | 3         | 2         | 1     |

### 3.5.4 Influence of Process Parameters on The Power Output

When examining the influence of each parameter on power output, VFD had the most substantial impact, with the highest Delta values of 10.90 for Means and 6.35 for S/N Ratios. This indicated that the power output was also highly sensitive to changes in the VFD setting. The pitch angles  $\beta_3$ ,  $\beta_2$ , and  $\beta_1$  follow in descending order of influence. The rankings confirmed that VFD was the most critical factor in optimizing power output. The pitch angles had a comparatively smaller, but still significant, impact. The consistency in the optimal parameter settings for both power output and shaft rotational speed underscored the interconnected nature of these performance metrics within the system.

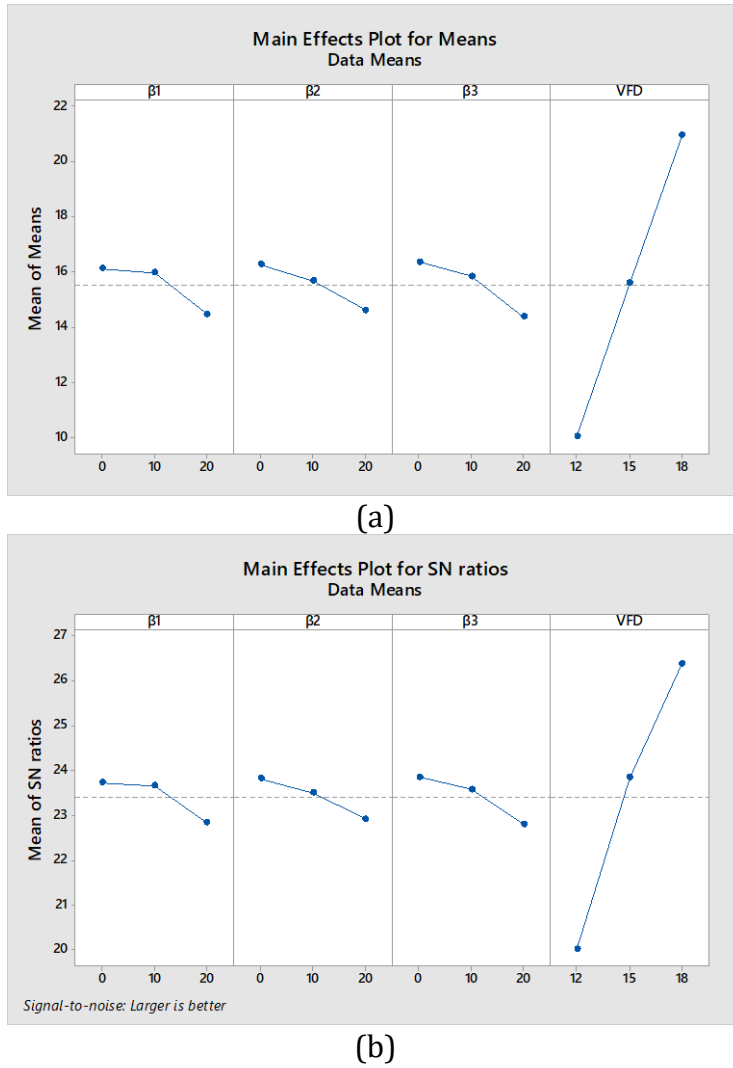


Fig. 9. Response graphs for power output: (a) Means, (b) Signal to Noise Ratios

3.5.5 Taguchi's Response Analysis for The Vibration Level

In the third case, the impact of process parameters  $\beta_1$ ,  $\beta_2$ ,  $\beta_3$ , and VFD on the vibration level was examined. Table 5 displays how variations in each factor affect the system's performance in terms of Mean and Signal to Noise Ratio values. The analysis revealed that the optimal set of process parameters, based on the lower-the-better criterion, was  $\beta_1$ -3,  $\beta_2$ -1,  $\beta_3$ -3, and VFD-1, ( $\beta_1=20^\circ$ ,  $\beta_2=0^\circ$ ,  $\beta_3=20^\circ$ , and VFD=12). Fig. 10 displays the response graphs for the rotating speed of Means and Signal to Noise Ratios.

Table 5. Response table for vibration level

| Level | Means     |           |           |        | Signal to Noise Ratios |           |           |        |
|-------|-----------|-----------|-----------|--------|------------------------|-----------|-----------|--------|
|       | $\beta_1$ | $\beta_2$ | $\beta_3$ | VFD    | $\beta_1$              | $\beta_2$ | $\beta_3$ | VFD    |
| 1     | 9.569     | 9.326     | 9.709     | 8.377  | -19.48                 | -19.22    | -19.61    | -18.34 |
| 2     | 9.679     | 9.718     | 9.686     | 9.504  | -19.56                 | -19.64    | -19.59    | -19.46 |
| 3     | 9.446     | 9.650     | 9.298     | 10.812 | -19.42                 | -19.60    | -19.26    | -20.66 |
| Delta | 0.234     | 0.392     | 0.411     | 2.435  | 0.14                   | 0.42      | 0.34      | 2.32   |
| Rank  | 4         | 3         | 2         | 1      | 4                      | 2         | 3         | 1      |

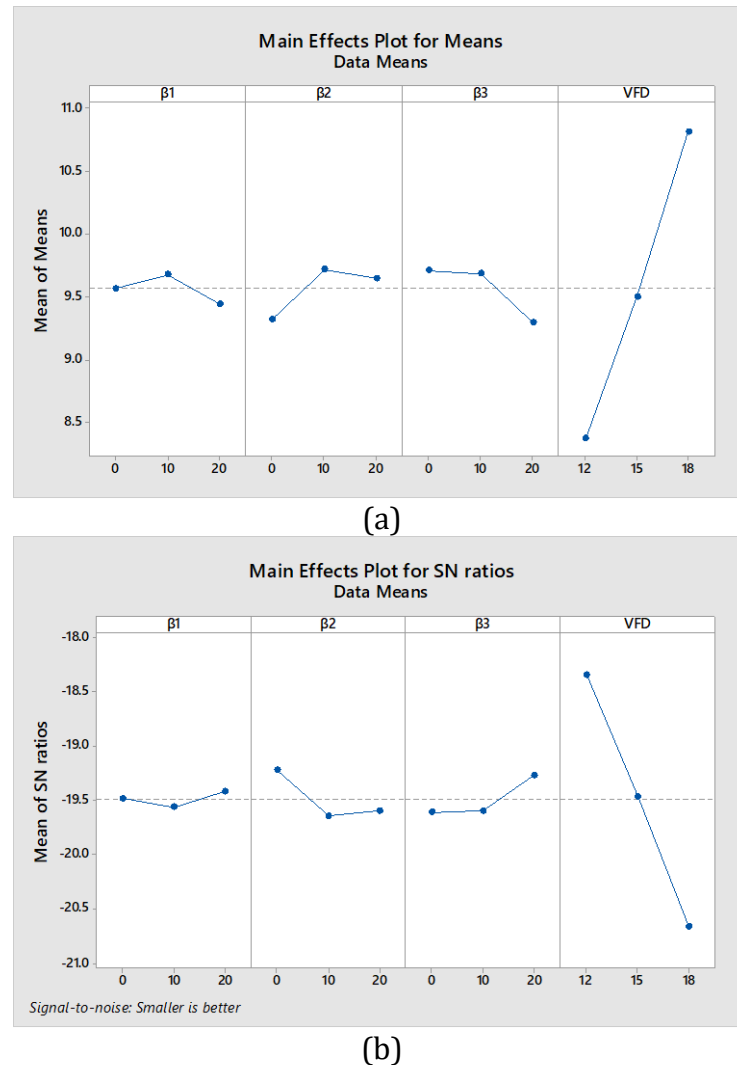


Fig. 10. Response graphs for vibration level (a) Means, (b) Signal to Noise Ratios

### 3.5.6 Influence of Process Parameters on The Vibration Level

When assessing the impact of each parameter on vibration levels, the VFD setting had again the most significant influence. It indicated the highest Delta values of 2.435 for Means and 2.32 for S/N Ratios. The vibration level is highly sensitive to changes in VFD also. The pitch angle  $\beta_3$  showed a slightly higher impact on vibration levels compared to  $\beta_2$  and  $\beta_1$ . This ranking emphasized that the blade pitch angles played a significant role, particularly  $\beta_3$ .

### 3.6 Analysis of Variance for Measured Performance

The analysis of variance (ANOVA) for the measured performance in wind turbine showed the significance of the input parameters on the system's responses. ANOVA was used on the performance measures at 95% confidence level and was computed using Minitab statistical software. In this context, ANOVA revealed that VFD was the more dominant factor influencing system responses. Due to balancing scenarios at which the rotational speed was affected, the P-values of the blade pitch angles input parameters were higher than 0.05, but still they created influence as shown in Fig. 7. Table 6 shows this analysis.

### 3.7 Regression Modelling Results

In this section, a regression analysis was conducted to quantify the relationship between input parameters (predictors) and system responses. Two types of regression models were developed to determine the best model fit for wind turbine performance, namely; linear model and full quadratic model. Minitab software was used in the regression analysis. Table 7 shows the input variables of

each model. The R-squared values of the developed models were compared to determine the best-fit model, as shown in Table 8.

Table 6. Analysis of variance (ANOVA) analysis

| Response                            | Source    | DF | Adj SS  | Adj MS  | F-Value | P-Value |
|-------------------------------------|-----------|----|---------|---------|---------|---------|
| Shaft rotational speed (rpm)        | $\beta_1$ | 2  | 743.4   | 371.7   | 44.15   | 0.000   |
|                                     | $\beta_2$ | 2  | 929.0   | 464.5   | 55.17   | 0.000   |
|                                     | $\beta_3$ | 2  | 1043.9  | 521.9   | 62.00   | 0.000   |
|                                     | VFD       | 2  | 31791.6 | 15895.8 | 1888.15 | 0.000   |
|                                     | Error     | 72 | 606.1   | 8.4     |         |         |
|                                     | Total     | 80 | 35114.0 |         |         |         |
| Power output (W)                    | $\beta_1$ | 2  | 44.92   | 22.460  | 35.51   | 0.000   |
|                                     | $\beta_2$ | 2  | 38.31   | 19.155  | 30.28   | 0.000   |
|                                     | $\beta_3$ | 2  | 56.79   | 28.396  | 44.89   | 0.000   |
|                                     | VFD       | 2  | 1605.03 | 802.515 | 1268.66 | 0.000   |
|                                     | Error     | 72 | 45.54   | 0.633   |         |         |
|                                     | Total     | 80 | 1790.60 |         |         |         |
| Vibration level (m/s <sup>2</sup> ) | $\beta_1$ | 2  | 0.737   | 0.3684  | 0.22    | 0.801   |
|                                     | $\beta_2$ | 2  | 2.372   | 1.1858  | 0.72    | 0.492   |
|                                     | $\beta_3$ | 2  | 2.885   | 1.4425  | 0.87    | 0.423   |
|                                     | VFD       | 2  | 80.220  | 40.1102 | 24.20   | 0.000   |
|                                     | Error     | 72 | 119.320 | 1.6572  |         |         |
|                                     | Total     | 80 | 205.534 |         |         |         |

Table 7. Regression models input parameters

| Regression model                                | Input variables  |
|---|--|
| Linear  | Linear: $\beta_1$ , $\beta_2$ , $\beta_3$ and VFD  |
| Full quadratic (Linear + Squared + Interaction) | Linear: $\beta_1$ , $\beta_2$ , $\beta_3$ and VFD<br>Squared: $\beta_1^2$ , $\beta_2^2$ , $\beta_3^2$ and VFD <sup>2</sup><br>Interaction: ( $\beta_1 \times \beta_2$ ), ( $\beta_2 \times \beta_3$ ), ( $\beta_3 \times \beta_1$ ), ( $\beta_1 \times \text{VFD}$ ), ( $\beta_2 \times \text{VFD}$ ), ( $\beta_3 \times \text{VFD}$ ) |

Table 8. R<sup>2</sup> values of various developed regression models

| Regression model                                | R <sup>2</sup> values (%) |                  |                                     |
|---|---------------------------|------------------|-------------------------------------|
|   | Rotational speed (rpm)    | Power output (W) | Vibration level (m/s <sup>2</sup> ) |
| Linear  | 97.76                     | 96.71            | 40.86                               |
| Full quadratic (Linear + Squared + Interaction) | 99.72                     | 99.33            | 44.89                               |

From the developed regression models shown in Table 10, the full quadratic model showed the best fit. The regression equations for the responses are:

$$\begin{aligned}
 \text{Rotational Speed} = & -56.71 + 0.854 \beta_1 + 0.957 \beta_2 + 1.144 \beta_3 + 16.330 \text{VFD} - 0.01333 \beta_1^2 - 0.01167 \beta_2^2 \\
 & - 0.01889 \beta_3^2 - 0.2037 \text{VFD}^2 - 0.00361 \beta_1 \beta_2 + 0.00139 \beta_2 \beta_3 - 0.00111 \beta_3 \beta_1 \\
 & - 0.06019 \beta_1 \text{VFD} - 0.07407 \beta_2 \text{VFD} - 0.07963 \beta_3 \text{VFD}
 \end{aligned}$$

$$\begin{aligned}
 \text{Power Output} &= -20.59 + 0.3165 \beta_1 + 0.2354 \beta_2 + 0.3254 \beta_3 + 2.722 \text{VFD} - 0.00674 \beta_1^2 \\
 &\quad - 0.00241 \beta_2^2 - 0.00469 \beta_3^2 - 0.0120 \text{VFD}^2 - 0.001434 \beta_1 \times \beta_2 - 0.000938 \beta_2 \times \beta_3 \\
 &\quad - 0.000129 \beta_3 \times \beta_1 - 0.01657 \beta_1 \times \text{VFD} - 0.01644 \beta_2 \times \text{VFD} - 0.02133 \beta_3 \times \text{VFD} \\
 \text{Vibration Level} &= 3.03 + 0.088 \beta_1 + 0.239 \beta_2 + 0.025 \beta_3 + 0.28 \text{VFD} - 0.00172 \beta_1^2 \\
 &\quad - 0.00230 \beta_2^2 - 0.00183 \beta_3^2 + 0.0101 \text{VFD}^2 + 0.00073 \beta_1 \times \beta_2 - 0.00052 \beta_2 \times \beta_3 \\
 &\quad + 0.00089 \beta_3 \times \beta_1 - 0.00505 \beta_1 \times \text{VFD} - 0.01194 \beta_2 \times \text{VFD} - 0.00082 \beta_3 \times \text{VFD}
 \end{aligned}$$

### 3.8 Performance Optimization

This section optimized the performance of the wind turbine system by balancing the system output responses. The optimization process utilized Grey Relational Analysis (GRA) in conjunction with a full factorial design in Minitab software. The optimization process resulted in defining the optimal settings of process parameters. The GRA focused on two primary criteria: maximizing the shaft rotational speed and power output (higher-the-better), and minimizing the vibration level (Lower-the-better). By applying these criteria, a Grey Relational Grade (GRG) was computed for each experimental test. Table 9 shows the calculated GRCs and GRG values, and ranking.

Table 9. Calculated GRCs and GRG values, and ranking

| Exp.      | Dependent Variables (Responses) |                 |               | Grey Relation Coefficients |                 |              | GRG          | Rank     |
|-----------|---------------------------------|-----------------|---------------|----------------------------|-----------------|--------------|--------------|----------|
|           | Rot. Speed                      | Vibration Level | Power Output  | Rot. Speed                 | Vibration Level | Power Output |              |          |
| 1         | 112                             | 6.274           | 10.730        | 0.379                      | 1.000           | 0.368        | 0.582        | 22       |
| 2         | 141                             | 10.106          | 17.430        | 0.545                      | 0.445           | 0.539        | 0.510        | 35       |
| <b>3</b>  | <b>171</b>                      | <b>10.326</b>   | <b>24.102</b> | <b>1.000</b>               | <b>0.431</b>    | <b>1.000</b> | <b>0.810</b> | <b>1</b> |
| 4         | 111                             | 6.943           | 10.643        | 0.375                      | 0.821           | 0.367        | 0.521        | 29       |
| 5         | 139                             | 11.238          | 16.898        | 0.529                      | 0.382           | 0.520        | 0.477        | 48       |
| <b>6</b>  | <b>168</b>                      | <b>10.849</b>   | <b>23.868</b> | <b>0.923</b>               | <b>0.402</b>    | <b>0.971</b> | <b>0.765</b> | <b>2</b> |
| 7         | 107                             | 7.486           | 10.237        | 0.360                      | 0.717           | 0.360        | 0.479        | 47       |
| 8         | 134                             | 10.239          | 16.014        | 0.493                      | 0.436           | 0.491        | 0.473        | 51       |
| 9         | 157                             | 10.411          | 21.164        | 0.720                      | 0.426           | 0.726        | 0.624        | 13       |
| 10        | 110                             | 7.400           | 10.701        | 0.371                      | 0.732           | 0.368        | 0.490        | 39       |
| 11        | 139                             | 11.402          | 17.290        | 0.529                      | 0.375           | 0.534        | 0.479        | 46       |
| <b>12</b> | <b>167</b>                      | <b>10.760</b>   | <b>23.868</b> | <b>0.900</b>               | <b>0.406</b>    | <b>0.971</b> | <b>0.759</b> | <b>3</b> |
| 13        | 109                             | 7.352           | 10.382        | 0.367                      | 0.740           | 0.362        | 0.490        | 40       |
| 14        | 137                             | 11.181          | 16.558        | 0.514                      | 0.385           | 0.508        | 0.469        | 57       |
| 15        | 164                             | 10.354          | 22.610        | 0.837                      | 0.429           | 0.839        | 0.702        | 5        |
| 16        | 106                             | 8.013           | 9.688         | 0.356                      | 0.638           | 0.351        | 0.449        | 70       |
| 17        | 131                             | 9.925           | 15.015        | 0.474                      | 0.457           | 0.462        | 0.464        | 62       |
| 18        | 153                             | 10.859          | 20.498        | 0.667                      | 0.401           | 0.684        | 0.584        | 20       |
| 19        | 107                             | 8.005           | 10.411        | 0.360                      | 0.639           | 0.363        | 0.454        | 67       |
| 20        | 135                             | 11.316          | 16.218        | 0.500                      | 0.378           | 0.497        | 0.459        | 66       |
| 21        | 159                             | 10.966          | 22.192        | 0.750                      | 0.396           | 0.803        | 0.650        | 9        |
| 22        | 107                             | 7.308           | 10.121        | 0.360                      | 0.748           | 0.358        | 0.489        | 42       |
| 23        | 132                             | 10.204          | 15.844        | 0.480                      | 0.439           | 0.486        | 0.468        | 59       |
| 24        | 155                             | 10.396          | 20.905        | 0.692                      | 0.427           | 0.709        | 0.609        | 15       |
| 25        | 103                             | 8.424           | 9.380         | 0.346                      | 0.588           | 0.346        | 0.427        | 72       |
| 26        | 126                             | 8.952           | 14.652        | 0.444                      | 0.534           | 0.452        | 0.477        | 49       |
| 27        | 143                             | 11.675          | 17.955        | 0.563                      | 0.362           | 0.559        | 0.495        | 37       |
| 28        | 110                             | 7.712           | 10.701        | 0.371                      | 0.681           | 0.368        | 0.473        | 52       |
| 29        | 139                             | 12.348          | 17.325        | 0.529                      | 0.336           | 0.535        | 0.467        | 60       |
| 30        | 166                             | 10.925          | 23.907        | 0.878                      | 0.398           | 0.976        | 0.750        | 4        |
| 31        | 108                             | 7.795           | 10.614        | 0.364                      | 0.669           | 0.366        | 0.466        | 61       |

Table 9 (continued)

| Exp | Dependent Variables (Responses) |                 |              | Grey Relation Coefficients |                 |              | GRG   | Rank |
|-----|---------------------------------|-----------------|--------------|----------------------------|-----------------|--------------|-------|------|
|     | Rot. Speed                      | Vibration Level | Power Output | Rot. Speed                 | Vibration Level | Power Output |       |      |
| 32  | 136                             | 12.325          | 16.660       | 0.507                      | 0.337           | 0.512        | 0.452 | 68   |
| 33  | 162                             | 11.423          | 23.028       | 0.800                      | 0.374           | 0.879        | 0.684 | 8    |
| 34  | 105                             | 6.774           | 10.295       | 0.353                      | 0.860           | 0.361        | 0.525 | 28   |
| 35  | 133                             | 7.052           | 15.576       | 0.486                      | 0.798           | 0.478        | 0.587 | 19   |
| 36  | 155                             | 10.072          | 21.090       | 0.692                      | 0.447           | 0.721        | 0.620 | 14   |
| 37  | 109                             | 10.528          | 10.701       | 0.367                      | 0.419           | 0.368        | 0.385 | 76   |
| 38  | 137                             | 7.474           | 16.762       | 0.514                      | 0.719           | 0.515        | 0.583 | 21   |
| 39  | 163                             | 12.156          | 23.400       | 0.818                      | 0.343           | 0.917        | 0.693 | 7    |
| 40  | 108                             | 10.750          | 10.498       | 0.364                      | 0.407           | 0.364        | 0.378 | 78   |
| 41  | 135                             | 7.739           | 16.422       | 0.500                      | 0.677           | 0.504        | 0.560 | 24   |
| 42  | 159                             | 11.469          | 22.306       | 0.750                      | 0.371           | 0.813        | 0.645 | 10   |
| 43  | 105                             | 10.872          | 10.092       | 0.353                      | 0.400           | 0.358        | 0.370 | 79   |
| 44  | 129                             | 8.217           | 15.180       | 0.462                      | 0.612           | 0.466        | 0.513 | 33   |
| 45  | 150                             | 9.910           | 20.424       | 0.632                      | 0.458           | 0.680        | 0.590 | 18   |
| 46  | 106                             | 11.462          | 10.353       | 0.356                      | 0.372           | 0.362        | 0.363 | 80   |
| 47  | 132                             | 8.174           | 15.980       | 0.480                      | 0.618           | 0.490        | 0.529 | 27   |
| 48  | 153                             | 10.679          | 20.831       | 0.667                      | 0.411           | 0.705        | 0.594 | 17   |
| 49  | 105                             | 11.416          | 10.237       | 0.353                      | 0.374           | 0.360        | 0.362 | 81   |
| 50  | 130                             | 8.378           | 15.312       | 0.468                      | 0.593           | 0.470        | 0.510 | 34   |
| 51  | 152                             | 10.309          | 22.572       | 0.655                      | 0.432           | 0.836        | 0.641 | 11   |
| 52  | 103                             | 7.490           | 9.240        | 0.346                      | 0.716           | 0.344        | 0.469 | 58   |
| 53  | 128                             | 7.599           | 14.080       | 0.456                      | 0.699           | 0.438        | 0.531 | 26   |
| 54  | 143                             | 10.287          | 17.710       | 0.563                      | 0.433           | 0.550        | 0.515 | 32   |
| 55  | 108                             | 6.916           | 10.440       | 0.364                      | 0.827           | 0.363        | 0.518 | 31   |
| 56  | 137                             | 10.124          | 16.558       | 0.514                      | 0.444           | 0.508        | 0.489 | 41   |
| 57  | 162                             | 9.982           | 22.534       | 0.800                      | 0.453           | 0.833        | 0.695 | 6    |
| 58  | 107                             | 7.081           | 10.237       | 0.360                      | 0.792           | 0.360        | 0.504 | 36   |
| 59  | 134                             | 9.469           | 15.444       | 0.493                      | 0.490           | 0.474        | 0.486 | 43   |
| 60  | 157                             | 9.675           | 20.905       | 0.720                      | 0.474           | 0.709        | 0.635 | 12   |
| 61  | 104                             | 8.354           | 9.660        | 0.350                      | 0.596           | 0.351        | 0.432 | 71   |
| 62  | 128                             | 8.630           | 14.652       | 0.456                      | 0.566           | 0.452        | 0.491 | 38   |
| 63  | 146                             | 11.268          | 18.720       | 0.590                      | 0.381           | 0.592        | 0.521 | 30   |
| 64  | 106                             | 7.744           | 10.034       | 0.356                      | 0.676           | 0.357        | 0.463 | 63   |
| 65  | 133                             | 9.940           | 15.378       | 0.486                      | 0.456           | 0.472        | 0.471 | 55   |
| 66  | 156                             | 10.647          | 20.646       | 0.706                      | 0.412           | 0.693        | 0.604 | 16   |
| 67  | 105                             | 7.942           | 9.520        | 0.353                      | 0.648           | 0.348        | 0.450 | 69   |
| 68  | 130                             | 9.354           | 14.916       | 0.468                      | 0.499           | 0.459        | 0.475 | 50   |
| 69  | 152                             | 10.513          | 20.128       | 0.655                      | 0.420           | 0.662        | 0.579 | 23   |
| 70  | 101                             | 8.862           | 9.184        | 0.340                      | 0.543           | 0.343        | 0.409 | 74   |
| 71  | 124                             | 8.772           | 13.760       | 0.434                      | 0.551           | 0.430        | 0.472 | 54   |
| 72  | 140                             | 12.254          | 17.535       | 0.537                      | 0.339           | 0.543        | 0.473 | 53   |
| 73  | 103                             | 8.976           | 9.296        | 0.346                      | 0.532           | 0.345        | 0.408 | 75   |
| 74  | 127                             | 8.951           | 14.718       | 0.450                      | 0.534           | 0.454        | 0.479 | 45   |
| 75  | 147                             | 10.863          | 19.152       | 0.600                      | 0.401           | 0.612        | 0.538 | 25   |
| 76  | 102                             | 8.739           | 9.100        | 0.343                      | 0.555           | 0.342        | 0.413 | 73   |
| 77  | 125                             | 8.912           | 13.952       | 0.439                      | 0.538           | 0.434        | 0.470 | 56   |



Table 9 (continued)

| Exp | Dependent Variables (Responses) |                 |              | Grey Relation Coefficients |                 |              | GRG   | Rank |
|-----|---------------------------------|-----------------|--------------|----------------------------|-----------------|--------------|-------|------|
|     | Rot. Speed                      | Vibration Level | Power Output | Rot. Speed                 | Vibration Level | Power Output |       |      |
| 78  | 142                             | 12.414          | 17.920       | 0.554                      | 0.333           | 0.558        | 0.482 | 44   |
| 79  | 99                              | 9.561           | 8.505        | 0.333                      | 0.483           | 0.333        | 0.383 | 77   |
| 80  | 119                             | 8.593           | 12.524       | 0.409                      | 0.570           | 0.402        | 0.460 | 64   |
| 81  | 133                             | 10.496          | 15.411       | 0.486                      | 0.421           | 0.473        | 0.460 | 65   |

The GRG combined the GRCs into a single performance score. Test 3 showed the highest GRG (0.810), making it the top rank, which means  $\beta_1=0^\circ$ ,  $\beta_2=0^\circ$ ,  $\beta_3=0^\circ$  and VFD=18. This indicated the best overall performance. With higher GRG achieved, test 3 was the best balance between power output and vibration control, making it a more optimal scenario. The optimal setting for system performance is shown in Table 10. The regression equation for GRG is:

$$GRG = 0.933 + 0.00757 \beta_1 + 0.00034 \beta_2 + 0.01168 \beta_3 - 0.0928 VFD - 0.000111 \beta_1^2 + 0.000032 \beta_2^2 - 0.000070 \beta_3^2 + 0.00466 VFD^2 + 0.000011 \beta_1 \times \beta_2 + 0.000079 \beta_2 \times \beta_3 + 0.000044 \beta_3 \times \beta_1 - 0.000566 \beta_1 \times VFD - 0.000361 \beta_2 \times VFD - 0.000941 \beta_3 \times VFD$$

Table 10. Optimal setting for system performance analysis

| Parameters and levels               | Optimal setting  |
|-------------------------------------|--|
|                                     | $\beta_1=0^\circ$ , $\beta_2=0^\circ$ , $\beta_3=0^\circ$ and VFD=18 |
| Shaft rotational speed (rpm)        | 171  |
| Power output (W)                    | 24.102   |
| Vibration level (m/s <sup>2</sup> ) | 10.326   |
| Grey Relational Grade               | 0.810  |

#### 4. Conclusion

This study conducted a comprehensive investigation into the impact of varying blade pitch angles and Variable Frequency Drive (VFD) settings on the performance characteristics of a wind turbine system. Using the Spectra Quest Wind Turbine Simulator (SQ WTS), a systematic experimental approach, grounded in Taguchi's method, was implemented to evaluate the influence of these variables on critical metrics, including shaft rotational speed, power output, and vibration levels. A total of 81 experiments were designed to capture the interactions between different pitch angles and VFD settings, revealing that these factors significantly influence the operational efficiency of wind turbines.

The results highlighted that an optimal combination of lower blade pitch angles (0°) and higher VFD settings (18) achieved the best performance, with a peak shaft rotational speed of 171 rpm and a maximum power output of 24.102 W, while maintaining vibration levels within acceptable limits. Conversely, increasing blade pitch angles introduced higher air resistance, negatively impacting rotational speed and power output. Some specific combinations of pitch angles, however, demonstrated a unique balancing effect, reducing vibration while maintaining satisfactory power levels, suggesting potential avenues for refining wind turbine design to optimize performance.

Furthermore, the main two regression models developed highlighted the critical role of VFD settings in enhancing system performance. This demonstrated that it is the most significant predictor for rotational speed and power output. Analysis of Variance (ANOVA) confirmed these findings, with VFD showing a dominant influence over system responses compared to blade pitch angles, which still contributed to performance variation. Mostly, in the balancing scenarios.

The optimization process employing Grey Relational Analysis (GRA) technique identified the optimal operating condition that maximized power output while minimizing vibration. This underscored the potential for future operational guidelines in wind turbine design and management. These insights not only contributed to the foundational knowledge of wind turbine

performance dynamics, but also served as a basis for future research targeting improved efficiency and sustainability in wind energy technology.

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